

Multiple-Treatments Meta-Analysis

Dr Georgia Salanti & Sofia Dias

*With thanks to Julian Higgins, Tony Ades, Andrea Cipriani, Corrado Barbui
University of Ioannina
Greece*

Outline – Part I

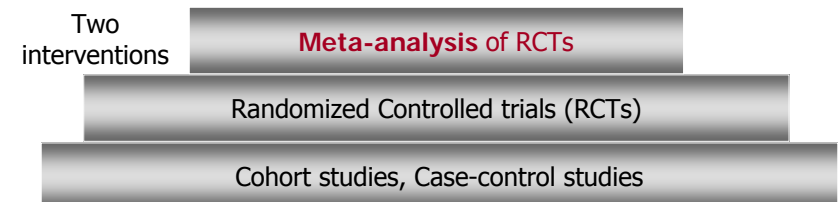
- Concept
- Simple indirect comparison
- Advantages of the methods
- MTM using frequentist meta-regression
- Presentation of results
- The notion of Inconsistency

Outline – Part II

- Bayesian MTM model
- Comparison of models

Evidence Based Medicine

- Backbone: **meta-analysis**
- Rigorous statistical models
- Clinical practice guidelines
 - NICE, WHO, The Cochrane Collaboration, HuGENet



Levels of evidence For Therapy, Prevention, Aetiology and Harm
Centre for Evidence Based Medicine, University of Oxford

12 new generation antidepressants

19 **meta-analyses** published in the last two years

"Although **Mirtazapine** is likely to have a faster onset of action than **Sertraline and Paroxetine** no significant differences were observed..."

"...statistically significant differences in terms of efficacy between **Fluoxetine and Venlafaxine**, but the clinical meaning of these differences is uncertain..."

"...**meta-analysis** highlighted a trend in favour of **Sertraline** over other **Fluoxetine**"

"**Venlafaxine** tends to have a favorable trend in response rates compared with **duloxetine**"

Fluoxetine: 28€ Venlafaxine:111€ Sertaline: 76 €

12 new generation antidepressants

19 **meta-analyses** published in the last two years

- paroxetine — reboxetine
- duloxetine — mirtazapine
- escitalopram — fluvoxamine
- milnacipran — citalopram
- sertraline — venlafaxine
- bupropion — fluoxetine
- milnacipran — paroxetine
- sertraline ? duloxetine
- bupropion — escitalopram
- fluvoxamine — milnacipran

12 new generation antidepressants

19 **meta-analyses** published in the last two years

paroxetine — reboxetine	paroxetine	0%	Probability to be the best
duloxetine — mirtazapine	sertraline	7%	
escitalopram — fluvoxamine	citalopram	0%	
milnacipran — citalopram	escitalopram	26%	
sertraline — venlafaxine	fluoxetine	0%	
bupropion — fluoxetine	fluvoxamine	0%	
milnacipran — paroxetine	milnacipran	1%	
sertraline ? duloxetine	venlafaxine	11%	
bupropion — escitalopram	reboxetine	0%	
fluvoxamine — milnacipran	bupropion	0%	
	mirtazapine	54%	
	duloxetine	0%	

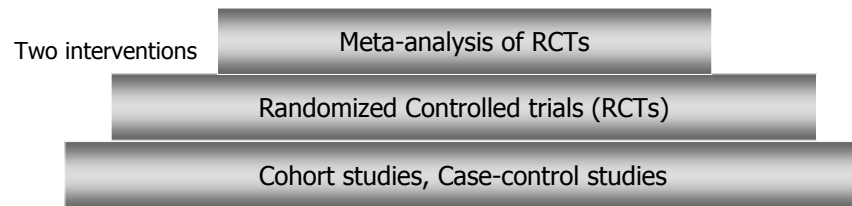
12 new generation antidepressants

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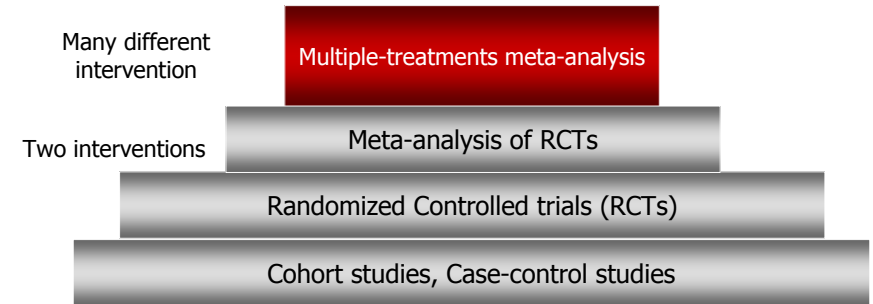
paroxetine reboxetine	paroxetine	0%	Probability to be the best
duloxetine mirtazapine	sertraline	7%	
escitalopram fluvoxamine	citalopram	0%	
milnacipran — citalopram	escitalopram	26%	
sertraline — venlafaxine	fluoxetine	0%	
bupropion — fluoxetine	fluvoxamine	0%	
milnacipran — paroxetine	milnacipran	1%	
sertraline? duloxetine	venlafaxine	11%	
bupropion escitalopram	reboxetine	0%	
fluvoxamine milnacipran	bupropion	0%	
	mirtazapine	54%	
	duloxetine	0%	

Current meta-analysis misses data!

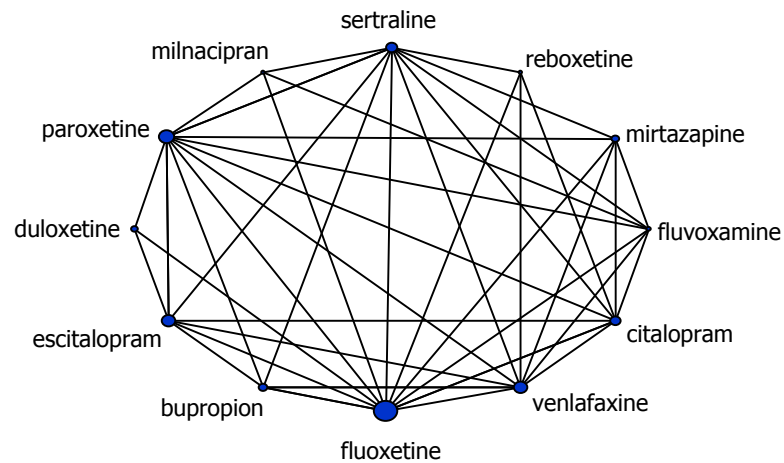
A new methodological framework



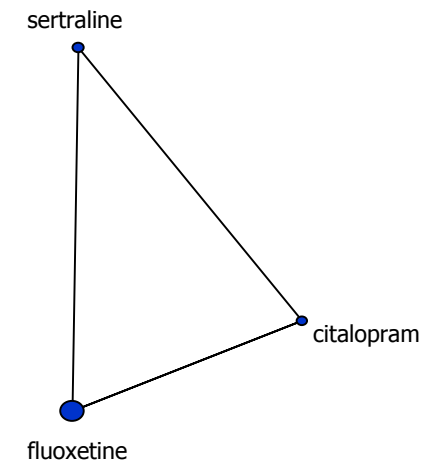
A new methodological framework



Network of experimental comparisons

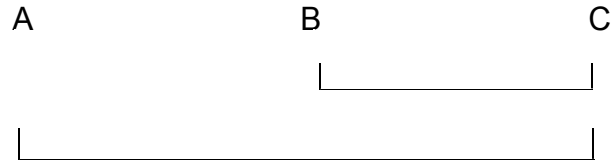


Network of experimental comparisons



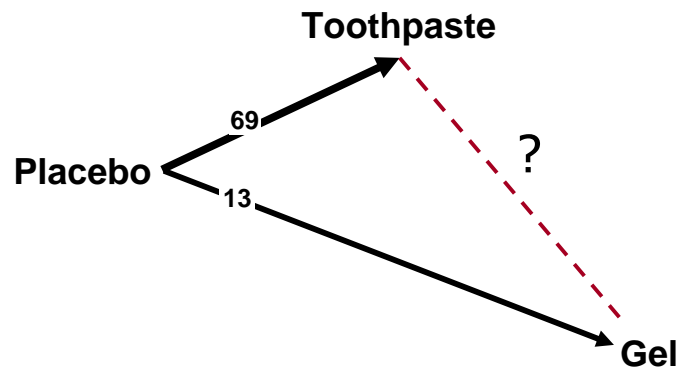
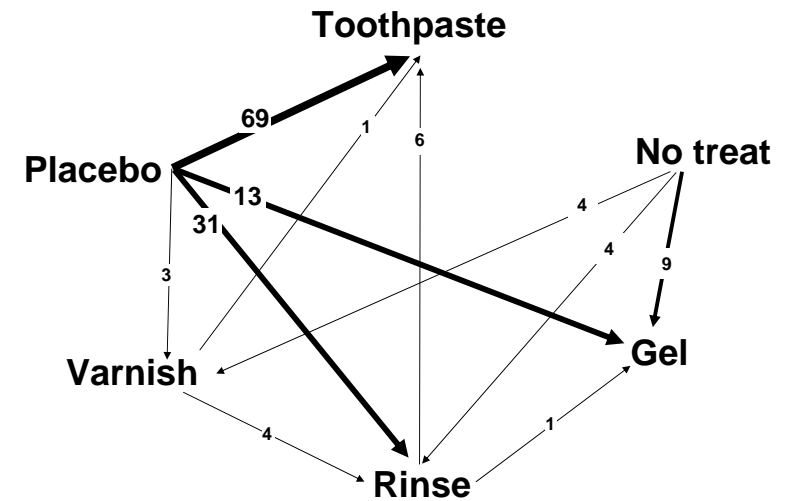
Indirect comparison

- We can obtain an *indirect estimate* for A vs B from RCTs comparing A vs C and B vs C:

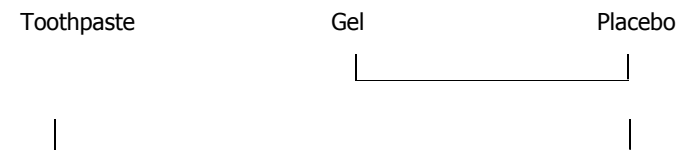


$$MD_{AB} = MD_{AC} - MD_{BC}$$

$$Var(MD_{AB}) = Var(MD_{AC}) + Var(MD_{BC})$$



Simple exercise: prevented mean caries



Comparison	MD	CI
Placebo vs Toothpaste	-0.34	(-0.41, -0.28)
Placebo vs Gel	-0.19	(-0.30, -0.10)

How to compare Gel to Toothpaste?

Estimate indirect MD and a 95% CI

Flash back to stats...

Each estimate has uncertainty as conveyed by the variance, the standard error and the 95% CI

Variance = SE²

95% CI (Low CI, High CI): $x - 1.96 \cdot SE$ to $x + 1.96 \cdot SE$:

SE = (High CI - Low CI) / 3.92

Pen and paper (and calculator!) exercise!

$$\text{Indirect } MD_{GvsT} = MD_{PvsT} - MD_{PvsG}$$

$$\text{Indirect } MD_{GvsT} = -0.34 - (-0.19) = -0.15$$

$$\text{Variance Indirect } MD_{GvsT} = \text{Variance } MD_{PvsT} + \text{Variance } MD_{PvsG}$$

$$\text{Variance } MD_{PvsT} = ((\text{high CI} - \text{low CI}) / 3.92)^2$$

$$\text{Variance } MD_{PvsT} = ((-0.28 - (-0.41)) / 3.92)^2 = 0.0011$$

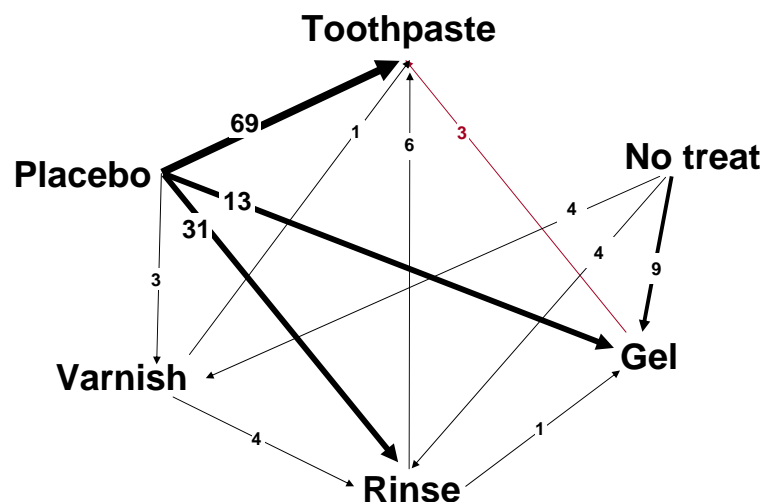
$$\text{Variance } MD_{GvsT} = ((-0.10 - (-0.30)) / 3.92)^2 = 0.0026$$

$$\text{Variance Indirect } MD_{GvsT} = 0.0011 + 0.0026 = 0.0037$$

$$\text{SE Indirect } MD_{GvsT} = \sqrt{0.0037} = 0.061$$

$$\text{95\% CI for Indirect } MD_{GvsT} = (-0.15 - 1.96 \cdot 0.061, -0.15 + 1.96 \cdot 0.061)$$

$$\text{95\% CI for Indirect } MD_{GvsT} = (-0.27, -0.03)$$



Combining direct and indirect evidence

- Inverse variance method
- Each estimate is 'weighted' by the inverse of the variance
- Then a common (pooled) result is obtained!

$$\text{pooled MD} = \frac{\frac{1}{\text{var}_{\text{Direct}}} MD_{\text{Direct}} + \frac{1}{\text{var}_{\text{Indirect}}} MD_{\text{Indirect}}}{\frac{1}{\text{var}_{\text{Direct}}} + \frac{1}{\text{var}_{\text{Indirect}}}}$$

$$\text{pooled MD} = \frac{\frac{1}{0.011} 0.04 + \frac{-1}{0.0037} 0.15}{\frac{1}{0.011} + \frac{1}{0.037}}$$

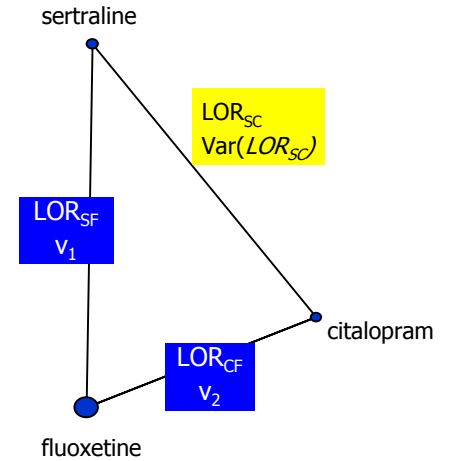
Indirect $MD_{GvST} = -0.15$
 Variance Indirect $MD_{GvST} = 0.0037$
 Direct $MD_{GvST} = 0.04$
 Variance Direct $MD_{GvST} = 0.011$

Pooled $MD_{GvST} = -0.14$

You can do this with any measure... InOR, InRR, RD, mean difference, HR, Peto's InOR etc...

Network of experimental comparisons

Indirect estimation
 $LOR_{SC} = LOR_{SF} - LOR_{CF}$
 $Var(LOR_{SC}) = v_1 + v_2$



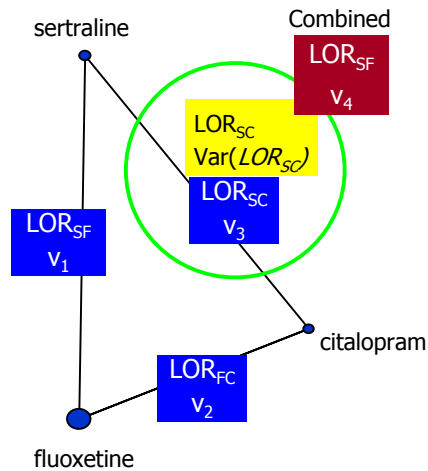
Lancet 2009 Cipriani, Fukurawa, Salanti et al

Network of experimental comparisons

Indirect estimation
 $LOR_{SC} = LOR_{SF} - LOR_{CF}$
 $Var(LOR_{SC}) = v_1 + v_2$

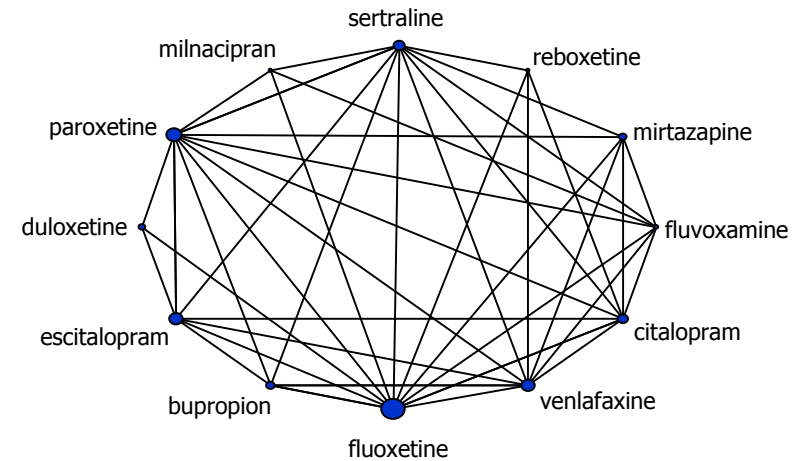
Combine the direct estimate with the indirect estimate using IV methods

Get a combined **LOR!**
 $v_4 < v_3$



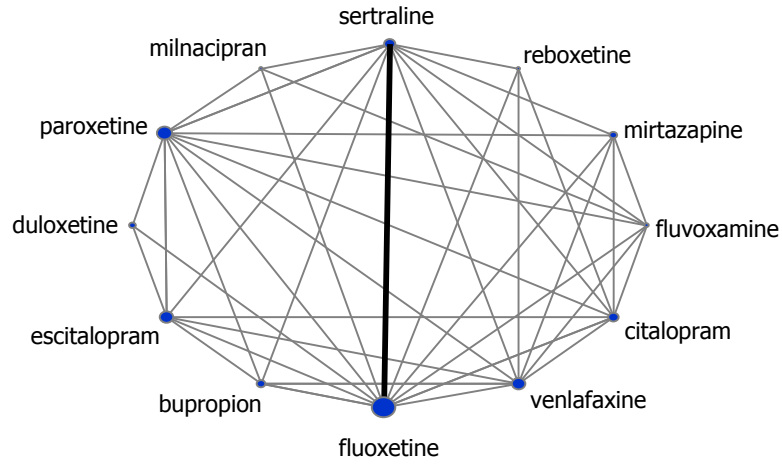
Lancet 2009 Cipriani, Fukurawa, Salanti et al

Network of experimental comparisons



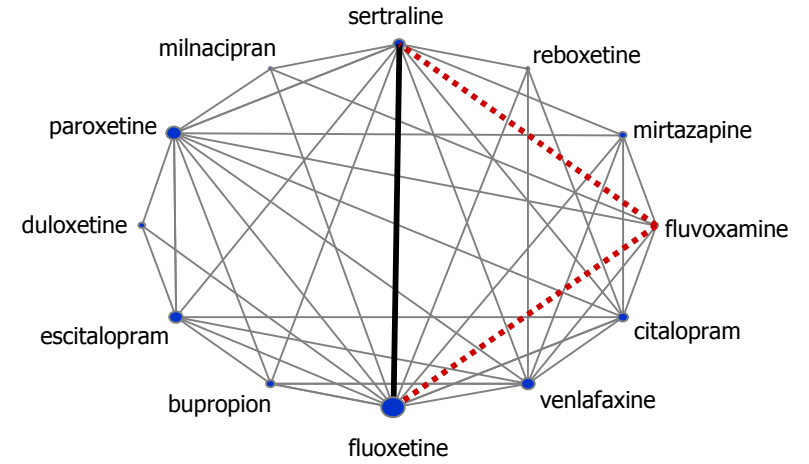
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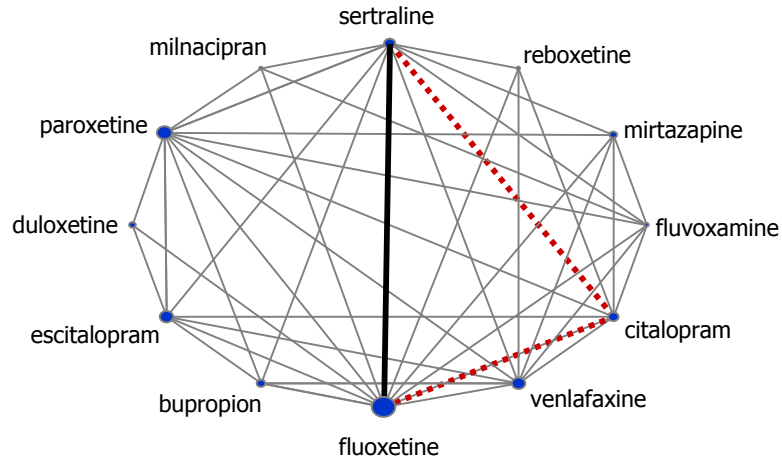
Lancet 2009 Cipriani, Fukurawa, Salanti et al

Network of experimental comparisons



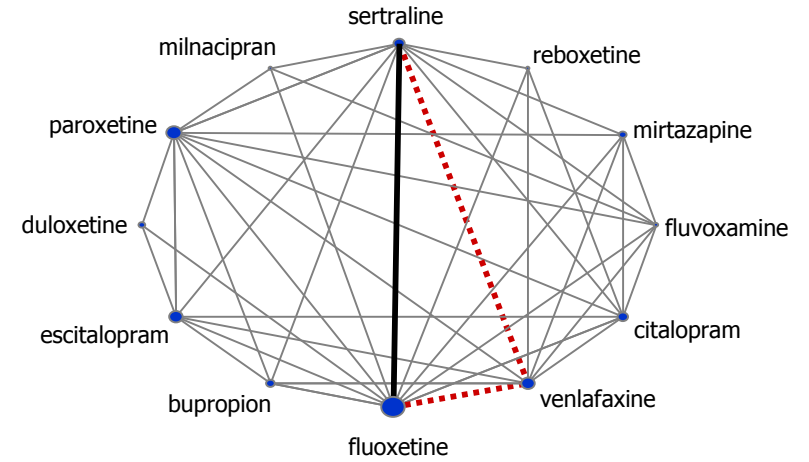
Lancet 2009 Cipriani, Fukurawa, Salanti et al

Network of experimental comparisons



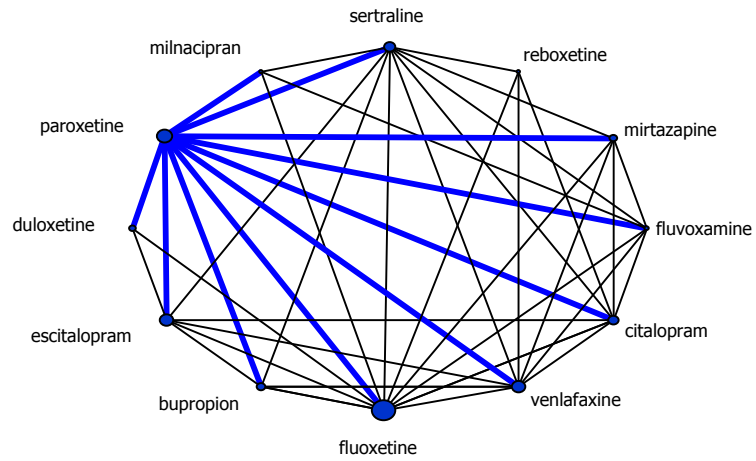
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Network of experimental comparisons

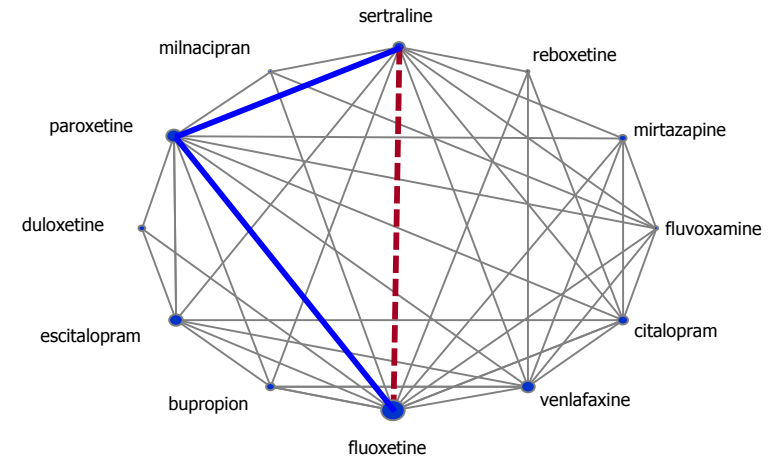


Lancet 2009 Cipriani, Fukurawa, Salanti et al

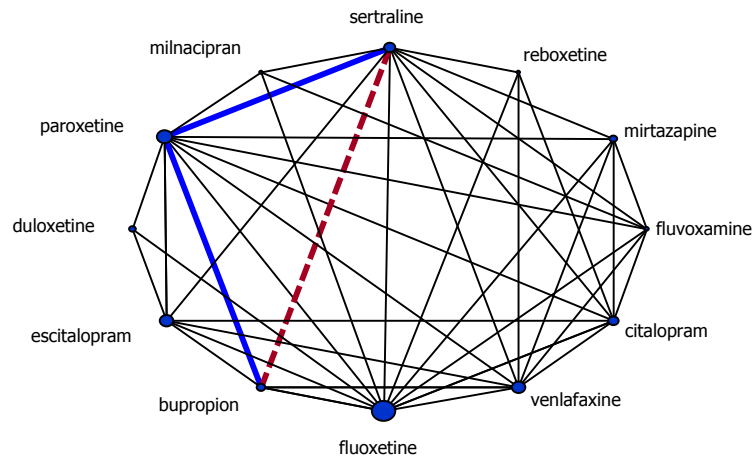
Choose basic parameters



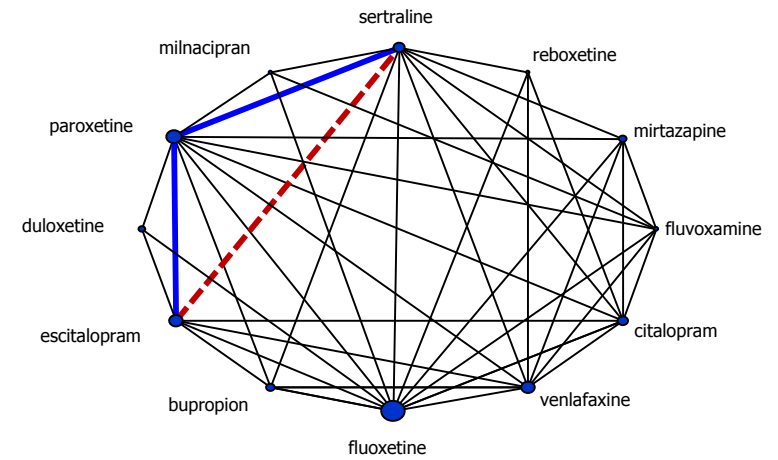
All other contrasts are functional!



All other contrasts are functional!



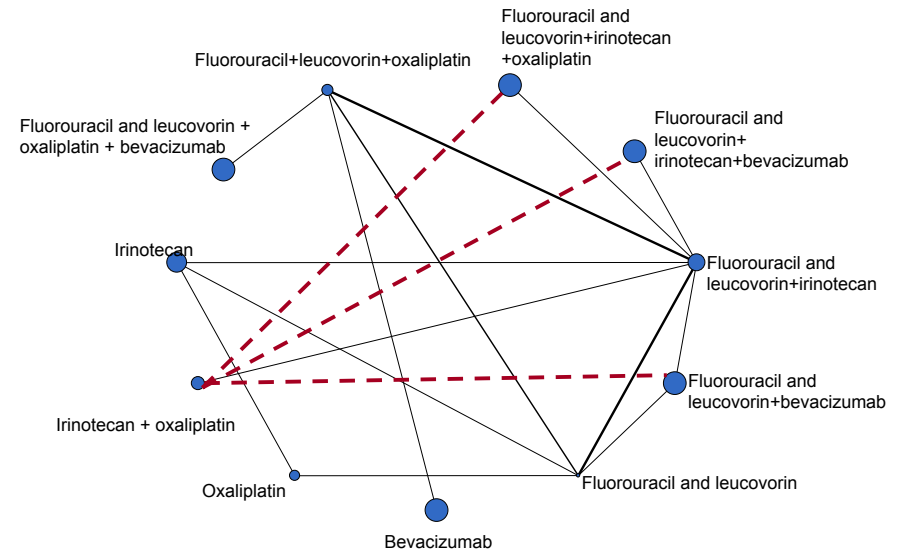
All other contrasts are functional!



Advantages of MTM

- Ranking of many treatments for the same condition (see later)
- Comprehensive use of all available data (indirect evidence)
- Comparison of interventions which haven't been directly compared in any experiment

Colorectal Cancer

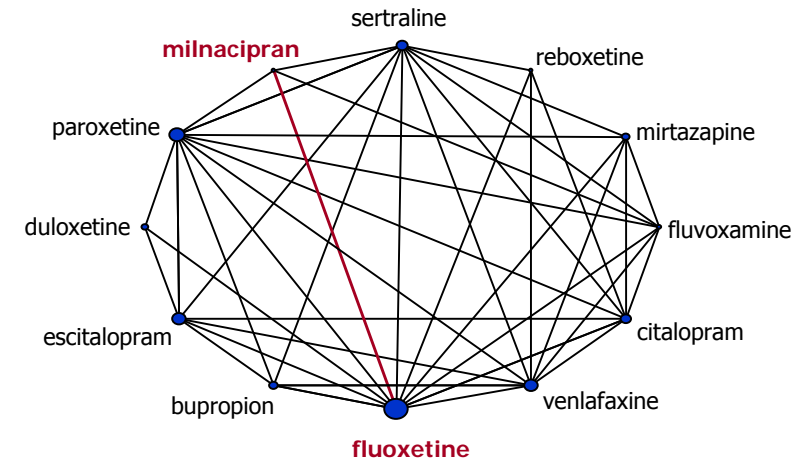


Gollinopoulos V, Salanti G, Pavlidis N, Ioannidis JP. Survival and disease-progression benefits with treatment regimens for advanced colorectal cancer: a meta-analysis. *Lancet Oncol* 2007; 8: 898-911.

Advantages of MTM

- Ranking of many treatments for the same condition (see later)
- Comprehensive use of all available data (indirect evidence)
- Comparison of interventions which haven't been directly compared in any experiment
- Improved precision for each comparison

Network of experimental comparisons



Fluoxetine vs Milnacipran (response to treatment)
 Meta-analysis: 1.15 (0.72, 1.85)
 MTM: 0.97 (0.69, 1.32)

Lancet 2009 Cipriani, Fukurawa, Salanti et al

Why use Bayesian statistics for meta-analysis?

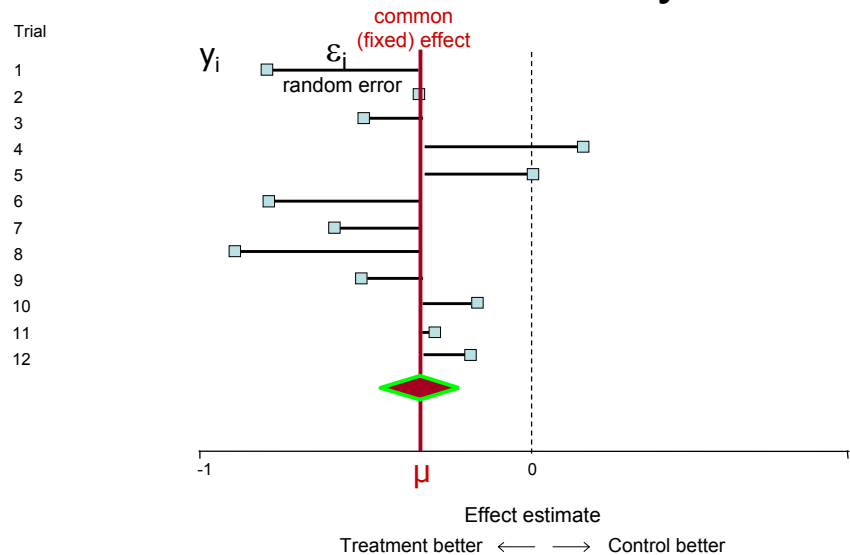
- **Natural approach for accumulating data**
- **Repeated updating of meta-analyses fine:** posterior should always reflect latest beliefs
- **People naturally think as Bayesians:** they have degrees of belief about the effects of treatment, which change when they see new data
- Probability statements about true effects of treatment easier to understand than confidence intervals and p -values

Why use Bayesian statistics for MTM?

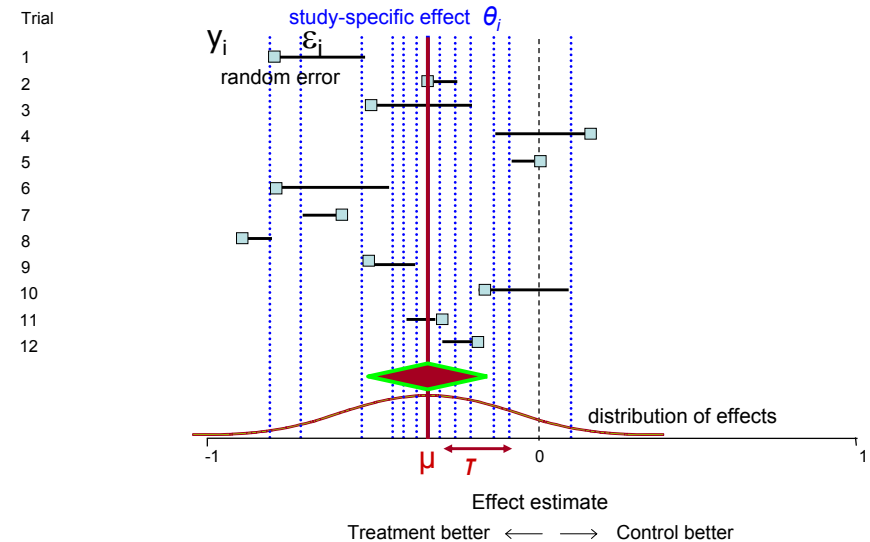
- Bayesian approach is **easier to account for correlations** induced by multi-arm trials
- Estimation of **predictive intervals** is straightforward
- Estimation of **ranking probabilities** is straightforward
- MTM with two-arm trials only (or ignoring the correlations)
Easy with frequentist meta-regression



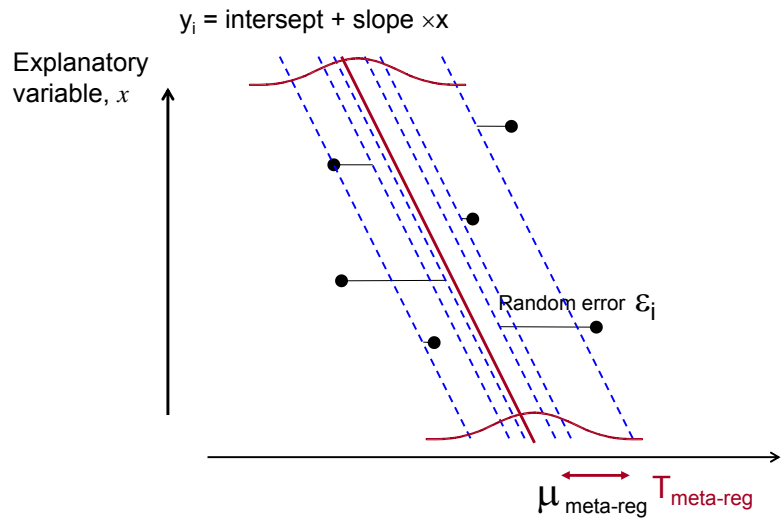
Fixed effect meta-analysis



Random effects meta-analysis



Random effects meta-regression



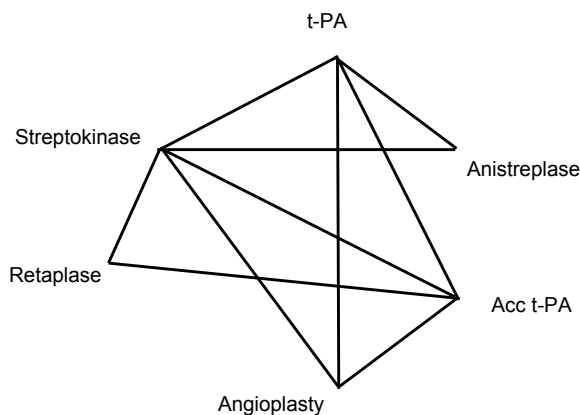
Meta-regression

- We observe y_i in each study (e.g. the $\log(\text{OR})$)
- Meta-regression using the treatments as 'covariates'
- AC, AB, BC studies, chose C as *reference*

$$y_i = \mu^{AC} \times (\text{Treat}_i=A) + \mu^{BC} \times (\text{Treat}_i=B)$$

- The AC studies have (1,0), the BC studies (0,1) [*basic*]
- AB studies have (1,-1) [*functional*]

Parametrisation of the network



Choose **basic parameters**
Write all other contrasts as linear functions of the basic parameters to build the design matrix

LOR for death in treatments for MI

LOR for death in treatments for MI

$$y_i = \mu^A \text{ t-PA} + \mu^B \text{ Anistreplase}_i + \mu^C \text{ Accelerated t-PA}_i + \mu^D \text{ Angioplasty}_i + \mu^E \text{ Reteplase}_i$$

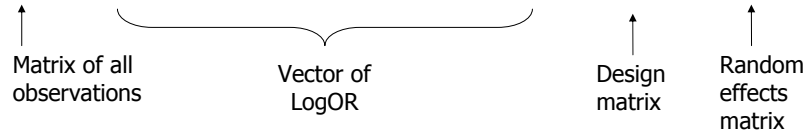
Use as 'covariates'

No. studies	Streptokinase	t-PA	Anistreplase	Acc t-PA	Angioplasty	Reteplase
3	1	1	0	0	0	0
1	1	0	1	0	0	0
1	1	0	0	1	0	0
3	1	0	0	0	1	0
1	1	0	0	0	0	1
1	1	-1	1	0	0	0
2	1	-1	0	0	1	0
2	1	0	0	-1	1	0
2	1	0	0	-1	0	1

LOR for death in treatments for MI

$$y_i = \mu^A \text{ t-PA} + \mu^B \text{ Anistreplase}_i + \mu^C \text{ Accelerated t-PA}_i + \mu^D \text{ Angioplasty}_i + \mu^E \text{ Reteplase}_i$$

$$Y = (\mu^A, \mu^B, \mu^C, \mu^D, \mu^E) \times X + \Delta$$



$$Y \sim N(\mu X, V) \quad \Delta \sim N(0, \text{diag}(\tau^2))$$

Variance-covariance matrix (for the observed LOR)

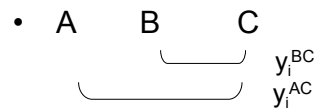
LOR compared to Streptokinase (RE model)

$$Y = (\mu^A, \mu^B, \mu^C, \mu^D, \mu^E) \times X + \Delta$$

Treatment	LOR (SE)	OR	95% CI
t-PA	-0.02 (0.03)	0.98	(0.92, 1.04)
Anistreplase	-0.00 (0.03)	1.00	(0.94, 1.06)
Accelerated t-PA	-0.15 (0.05)	0.86	(0.78, 0.95)
Angioplasty	-0.43 (0.20)	0.65	(0.44, 0.96)
Reteplase	-0.11 (0.06)	0.90	(0.80, 1.01)

What's the problem with multi-arm trials?

- We need to take into account the correlations between the estimates that come from the same study



- The random effects (θ_i^{BC} , θ_i^{AC}) that refer to the same trial are correlated as well
- You have to built in *the correlation matrix for the observed effects, and the correlation matrix for the random effects*

$$Y \sim N(\mu X, V) \quad \Delta \sim N(0, \text{diag}(\tau^2))$$

Hypothetical example

Study	No. arms	#	Data	Contrast
i=1	T ₁ =2	1	y _{1,1} , v _{1,1}	AB
i=2	T ₂ =2	1	y _{2,1} , v _{2,1}	AC
i=3	T ₃ =2	1	y _{3,1} , v _{3,1}	BC
i=4	T ₄ =3	2	y _{4,1} , v _{4,1} y _{4,2} , v _{4,2} cov(y _{4,1} , y _{4,2})	AB AC

Basic parameters: AB and AC

Study	No. arms	#	Data	Contrast
i=1	T ₁ =2	1	y _{1,1} , v _{1,1}	AB
i=2	T ₂ =2	1	y _{2,1} , v _{2,1}	AC
i=3	T ₃ =2	1	y _{3,1} , v _{3,1}	BC
i=4	T ₄ =3	2	y _{4,1} , v _{4,1} y _{4,2} , v _{4,2} cov(y _{4,1} , y _{4,2})	AB AC

Meta-regression

$$\begin{pmatrix} y_{1,1} \\ y_{2,1} \\ y_{3,1} \\ y_{4,1} \\ y_{4,2} \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \\ -1 & 1 \\ 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} \mu_{AB} \\ \mu_{AC} \end{pmatrix} + \begin{pmatrix} \beta_{1,1} \\ \beta_{2,1} \\ \beta_{3,1} \\ \beta_{4,1} \\ \beta_{4,2} \end{pmatrix} + \begin{pmatrix} \varepsilon_{1,1} \\ \varepsilon_{2,1} \\ \varepsilon_{3,1} \\ \varepsilon_{4,1} \\ \varepsilon_{4,2} \end{pmatrix}$$

Study	No. arms	#	Data	Contrast
i=1	T ₁ =2	1	y _{1,1} , v _{1,1}	AB
i=2	T ₂ =2	1	y _{2,1} , v _{2,1}	AC
i=3	T ₃ =2	1	y _{3,1} , v _{3,1}	BC
i=4	T ₄ =3	2	y _{4,1} , v _{4,1} y _{4,2} , v _{4,2} cov(y _{4,1} , y _{4,2})	AB AC

$$\begin{pmatrix} y_{1,1} \\ y_{2,1} \\ y_{3,1} \\ y_{4,1} \\ y_{4,2} \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \\ -1 & 1 \\ 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} \mu_{AB} \\ \mu_{AC} \end{pmatrix} + \begin{pmatrix} \beta_{1,1} \\ \beta_{2,1} \\ \beta_{3,1} \\ \beta_{4,1} \\ \beta_{4,2} \end{pmatrix} + \begin{pmatrix} \varepsilon_{1,1} \\ \varepsilon_{2,1} \\ \varepsilon_{3,1} \\ \varepsilon_{4,1} \\ \varepsilon_{4,2} \end{pmatrix}$$

Take into account correlation in observations

$$\begin{pmatrix} \varepsilon_{1,1} \\ \varepsilon_{2,1} \\ \varepsilon_{3,1} \\ \varepsilon_{4,1} \\ \varepsilon_{4,2} \end{pmatrix} \sim N \left(\begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} v_{1,1} & 0 & 0 & 0 & 0 \\ 0 & v_{2,1} & 0 & 0 & 0 \\ 0 & 0 & v_{3,1} & 0 & 0 \\ 0 & 0 & 0 & v_{4,1} & \text{cov}(y_{4,1}, y_{4,2}) \\ 0 & 0 & 0 & \text{cov}(y_{4,1}, y_{4,2}) & v_{4,2} \end{pmatrix} \right)$$

Study	No. arms	#	Data	Contrast
i=1	T ₁ =2	1	y _{1,1} , v _{1,1}	AB
i=2	T ₂ =2	1	y _{2,1} , v _{2,1}	AC
i=3	T ₃ =2	1	y _{3,1} , v _{3,1}	BC
i=4	T ₄ =3	2	y _{4,1} , v _{4,1} y _{4,2} , v _{4,2} cov(y _{4,1} , y _{4,2})	AB AC

$$\begin{pmatrix} y_{1,1} \\ y_{2,1} \\ y_{3,1} \\ y_{4,1} \\ y_{4,2} \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \\ -1 & 1 \\ 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} \mu_{AB} \\ \mu_{AC} \end{pmatrix} + \begin{pmatrix} \beta_{1,1} \\ \beta_{2,1} \\ \beta_{3,1} \\ \beta_{4,1} \\ \beta_{4,2} \end{pmatrix} + \begin{pmatrix} \varepsilon_{1,1} \\ \varepsilon_{2,1} \\ \varepsilon_{3,1} \\ \varepsilon_{4,1} \\ \varepsilon_{4,2} \end{pmatrix}$$

Take into account correlation in random effects

$$\begin{pmatrix} \beta_{1,1} \\ \beta_{2,1} \\ \beta_{3,1} \\ \beta_{4,1} \\ \beta_{4,2} \end{pmatrix} \sim N \left(\begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} \tau_{AB}^2 & 0 & 0 & 0 & 0 \\ 0 & \tau_{AC}^2 & 0 & 0 & 0 \\ 0 & 0 & \tau_{BC}^2 & 0 & 0 \\ 0 & 0 & 0 & \tau_{AB}^2 & \text{cov}(\beta_{4,1}, \beta_{4,2}) \\ 0 & 0 & 0 & \text{cov}(\beta_{4,1}, \beta_{4,2}) & \tau_{AC}^2 \end{pmatrix} \right)$$

How to fit such a model?

- MLwiN
- SAS, R
- STATA using metan

Ranking measures from MTM

- With many treatments judgments based on pairwise effect sizes are difficult to make
- Example: Antidepressants

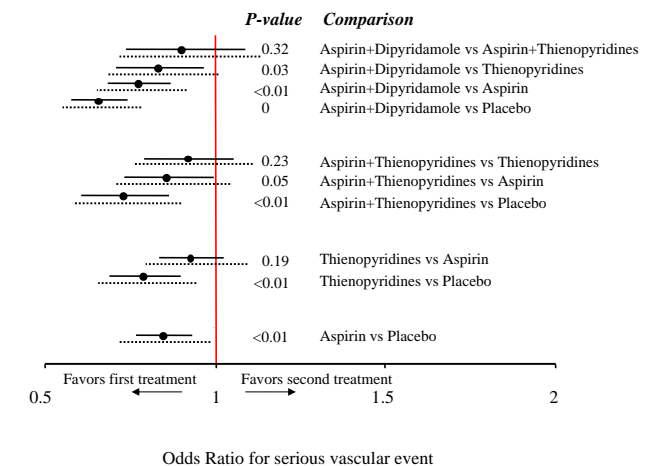
■ Efficacy (response rate) (95% CI) ■ Comparison □ Acceptability (dropout rate) (95% CI)

BUP	1.00 (0.78-1.28)	0.75 (0.55-1.01)	1.06 (0.86-1.32)	0.89 (0.74-1.08)	0.73 (0.53-1.00)	0.87 (0.58-1.24)	0.87 (0.66-1.14)	0.81 (0.65-1.00)	0.62 (0.45-0.86)	1.01 (0.82-1.27)	0.84 (0.68-1.02)
0.98 (0.78-1.23)	CIT	0.75 (0.55-1.02)	1.07 (0.86-1.31)	0.90 (0.73-1.09)	0.73 (0.54-0.99)	0.87 (0.60-1.24)	0.87 (0.66-1.15)	0.81 (0.65-1.01)	0.62 (0.45-0.84)	1.02 (0.81-1.28)	0.84 (0.67-1.06)
1.09 (0.83-1.43)	1.12 (0.87-1.44)	DUL	1.43 (1.09-1.85)	1.19 (0.91-1.57)	0.98 (0.67-1.41)	1.16 (0.77-1.73)	1.16 (0.83-1.61)	1.08 (0.84-1.40)	0.83 (0.57-1.22)	1.36 (1.01-1.83)	1.12 (0.84-1.50)
0.82 (0.67-1.01)	0.84 (0.70-1.01)	0.75 (0.60-0.93)	ESC	0.84 (0.70-1.01)	0.69 (0.50-0.94)	0.81 (0.55-1.15)	0.81 (0.62-1.07)	0.76 (0.62-0.93)	0.58 (0.43-0.81)	0.95 (0.77-1.19)	0.78 (0.64-0.97)
1.08 (0.90-1.29)	1.10 (0.93-1.31)	0.99 (0.79-1.24)	1.32 (1.12-1.55)	FLU	0.82 (0.62-1.07)	0.97 (0.69-1.32)	0.97 (0.77-1.21)	0.91 (0.79-1.05)	0.70 (0.53-0.92)	1.14 (0.96-1.36)	0.94 (0.81-1.09)
1.10 (0.83-1.47)	1.13 (0.86-1.47)	1.01 (0.74-1.38)	1.35 (1.02-1.76)	1.02 (0.81-1.30)	FVX	1.18 (0.76-1.75)	1.18 (0.87-1.61)	1.10 (0.84-1.47)	0.85 (0.57-1.26)	1.38 (1.03-1.89)	1.14 (0.86-1.54)
1.07 (0.77-1.48)	1.09 (0.78-1.50)	0.97 (0.69-1.38)	1.30 (0.95-1.78)	0.99 (0.74-1.31)	0.97 (0.68-1.37)	MIL	0.99 (0.69-1.53)	0.94 (0.68-1.31)	0.72 (0.48-1.10)	1.17 (0.84-1.72)	0.97 (0.69-1.40)
0.79 (0.72-1.00)	0.80 (0.63-1.01)	0.72 (0.54-0.94)	0.96 (0.76-1.19)	0.73 (0.60-0.88)	0.71 (0.55-0.92)	0.74 (0.53-1.01)	MIR	0.93 (0.75-1.17)	0.72 (0.51-1.03)	1.17 (0.91-1.51)	0.97 (0.76-1.23)
1.06 (0.87-1.30)	1.08 (0.90-1.30)	0.97 (0.78-1.20)	1.30 (1.10-1.53)	0.98 (0.86-1.12)	0.96 (0.76-1.23)	1.00 (0.74-1.33)	1.35 (1.11-1.64)	PAR	0.77 (0.56-1.05)	1.25 (1.04-1.52)	1.03 (0.86-1.24)
1.60 (1.20-2.16)	1.63 (1.25-2.14)	1.46 (1.05-2.02)	1.95 (1.47-2.59)	1.48 (1.16-1.90)	1.45 (1.03-2.02)	1.50 (1.03-2.18)	2.03 (1.52-2.78)	1.50 (1.16-1.98)	REB	1.63 (1.19-2.24)	1.34 (0.99-1.83)
0.87 (0.72-1.05)	0.88 (0.72-1.07)	0.79 (0.62-1.01)	1.06 (0.88-1.27)	0.80 (0.69-0.93)	0.79 (0.61-1.01)	0.81 (0.60-1.11)	1.10 (0.90-1.36)	0.82 (0.69-0.96)	0.54 (0.41-0.71)	SER	0.82 (0.67-1.00)
0.85 (0.70-1.01)	0.86 (0.71-1.05)	0.77 (0.60-0.99)	1.03 (0.86-1.24)	0.78 (0.68-0.90)	0.77 (0.59-0.99)	0.79 (0.58-1.08)	1.08 (0.87-1.33)	0.79 (0.67-0.94)	0.53 (0.40-0.69)	0.98 (0.82-1.16)	VEN

Ranking measures from MTM

- With many treatments judgments based on pairwise effect sizes are difficult to make
- Example: Antidepressants
- Example: Antiplatelet regimens for serious vascular events

Serious vascular events with antiplatelet regimens



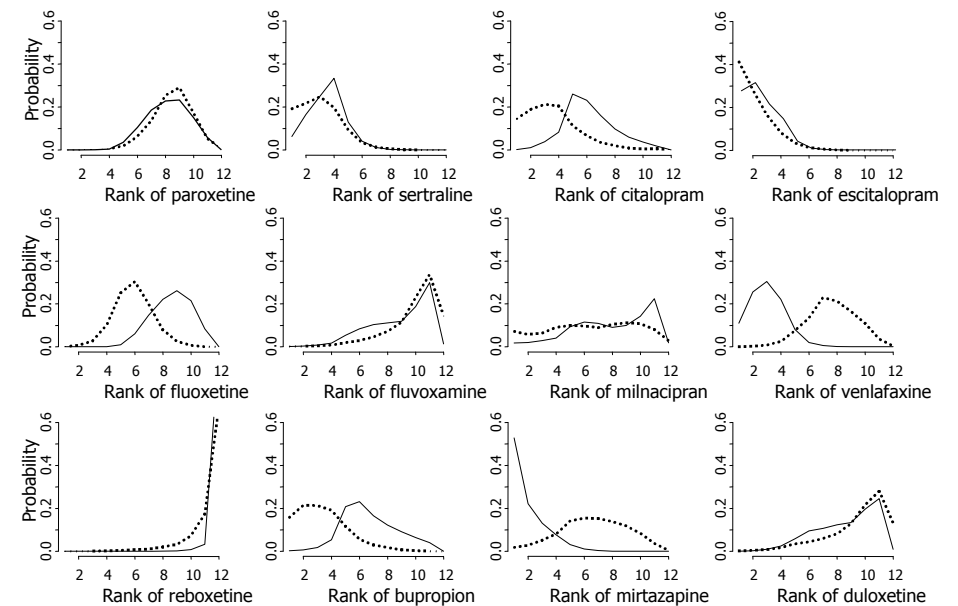
Probabilities instead of effect sizes

- Estimate for each treatment *the probability to be the best*
- This is straightforward within a Bayesian framework

% probability	A	B	C	D
$j=1$	0.25	0.50	0.25	0.00

% probability	A	B	C	D
$j=1$	0.25	0.50	0.25	0.00
$j=2$	0.25	0.25	0.50	0.00
$j=3$	0.25	0.25	0.25	0.25
$j=4$	0.25	0	0	0.75

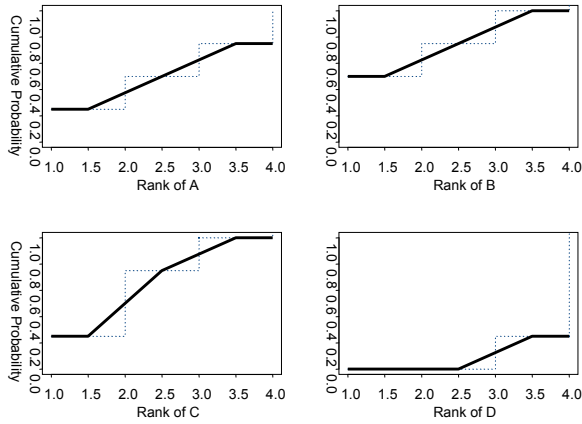
i the treatment
 j the rank



Ranking for efficacy (solid line) and acceptability (dotted line). Ranking: probability to be the best treatment, to be the second best, the third best and so on, among the 12 comparisons).

% probability	A	B	C	D
$j=1$	0.25	0.50	0.25	0.00
$j=2$	0.50	0.75	0.75	0.00
$j=3$	0.75	1.00	1.00	0.25
$j=4$	1.00	1.00	1.00	1.00

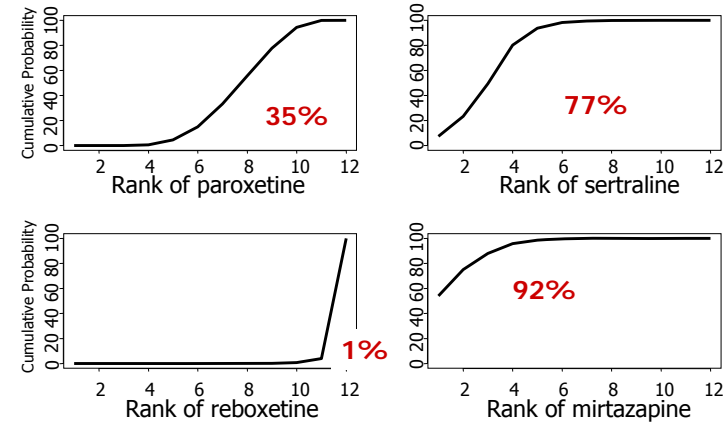
i the treatment
 j the rank



The areas under the cumulative curves for the four treatments of the example above are
A=0.5
B=0.75
C=0.67
D=0.08

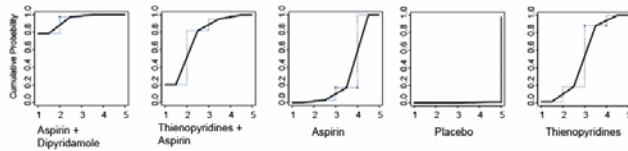
A comprehensive ranking measure

Preliminary results for ranking 12 antidepressants

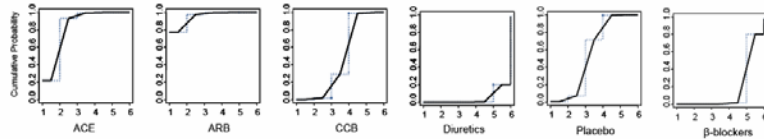


Compared to an imaginary antidepressant which is 'always the best', mirtazapine reaches up to 92% of its potential!

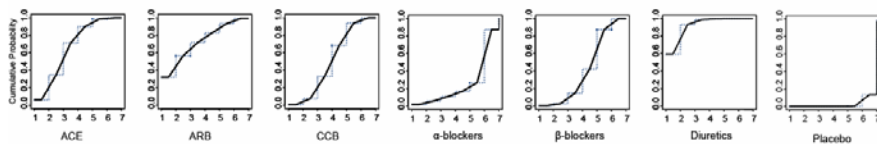
Serious vascular events with antiplatelet regimens



Incident diabetes with antihypertensive drugs



Serious cardiovascular event with antihypertensive drugs

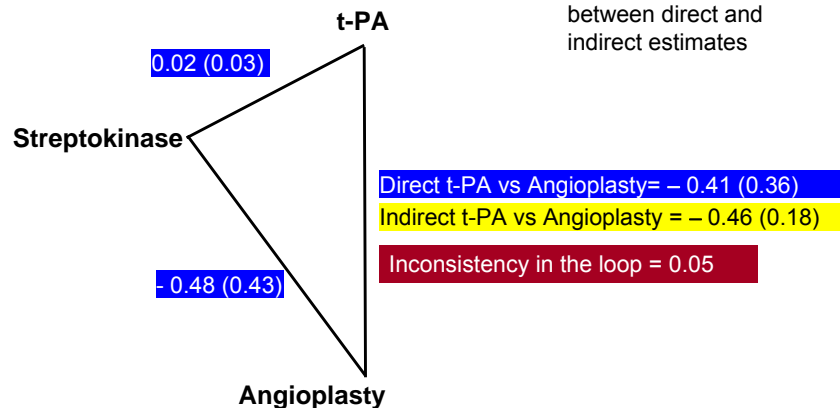


Inconsistency

- What is inconsistency?
- How it manifests itself?

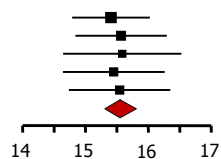
Inconsistency

LOR (SE) for MI

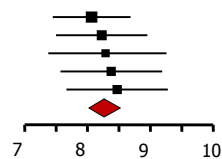


Inconsistency - Heterogeneity

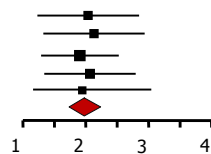
- **Heterogeneity**: 'excessive' discrepancy among study-specific effects
- **Inconsistency**: it is the excessive discrepancy among source-specific effects (direct and indirect)



AC=15.5



BC=8.2



AB=2.3

Inconsistency

Empirical Evidence

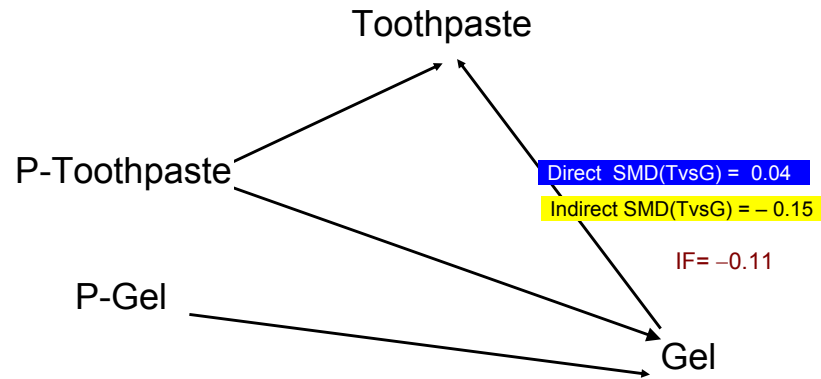
- In 3 cases out of 44 there was an important discrepancy between direct/indirect effect.
- Direction of the discrepancy is inconsistent

Glenny et al HTA 2005

What can cause inconsistency?

Inappropriate common comparator

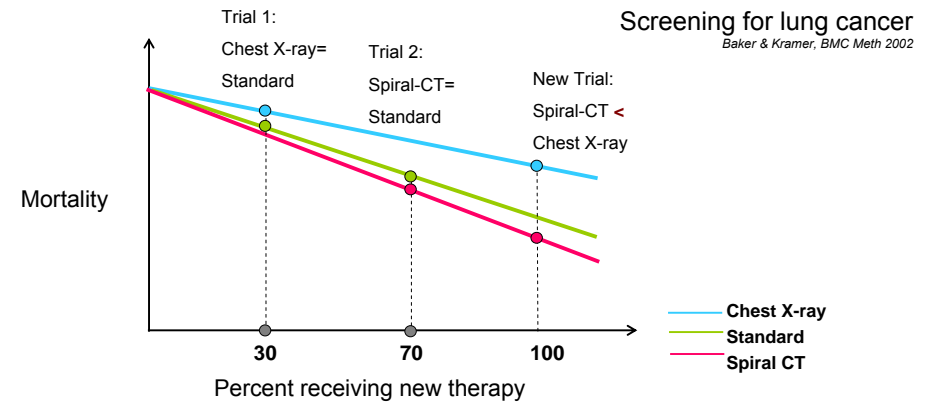
Compare Fluoride treatments in preventing dental caries



I cannot learn about Toothpaste versus Gel through Placebo!

What can cause inconsistency?

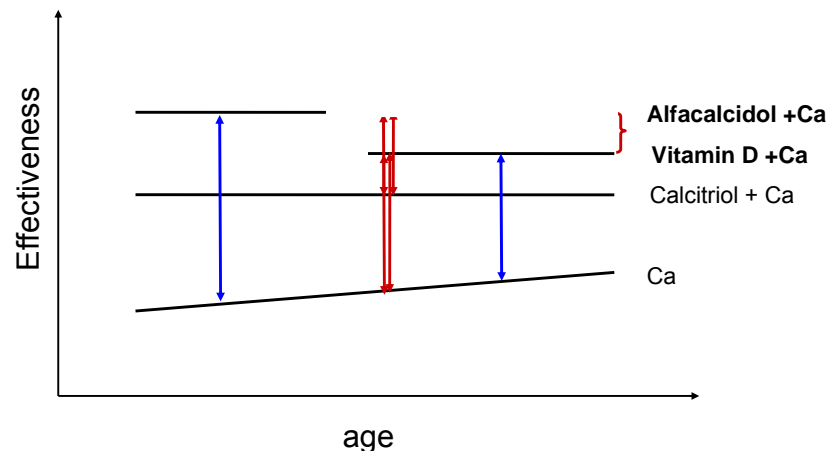
Confounding by trial characteristics



A new therapy (possibly unreported in the trials) decreases the mortality but in **different rates** for the three screening methods

What can cause inconsistency?

Confounding by trial characteristics



Different characteristics across comparisons may cause inconsistency

Assumptions of MTM

- There is **not confounding** by trial characteristics that are related to both the comparison being made and the magnitude of treatment difference
- The trials in two different comparisons are **exchangeable** (other than interventions being compared)
- Equivalent to the assumption '**the unobserved treatment is missing at random**'
 - Is this plausible?
 - Selection of the comparator is not often random!

Inconsistency

Detecting

- Check the distribution of important characteristics per treatment comparison
 - Usually unobserved....
 - **Time** (of randomization, of recruitment) might be associated with changes to the background risk that may violate the assumptions of MTM

Compare the characteristics!

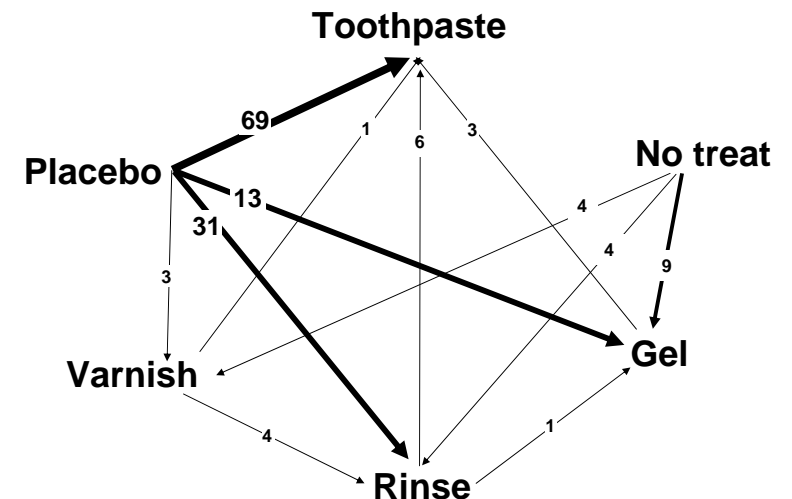
No. studies	T	G	R	V	P	Fup	Baseline	Year	Water F (yes/no)
69	■				■	2.6	11.8	1968	0.2
13		■			■	2.3	3.8	1973	0.2
30			■		■	2.4	5.9	1973	0.1
3				■	■	2.3	2.7	1983	0
3	■	■				2.7	NA	1968	0.66
6	■		■			2.8	14.7	1969	0
1	■			■		2	0.9	1978	0
1		■	■			1	NA	1977	0
1		■		■		3	7.4	1991	NA
4			■	■		2.5	7.6	1981	0.33

Salanti G, Marinho V, Higgins JP: A case study of multiple-treatments meta-analysis demonstrates that covariates should be considered. *J Clin Epidemiol* 2009, 62: 857-864.

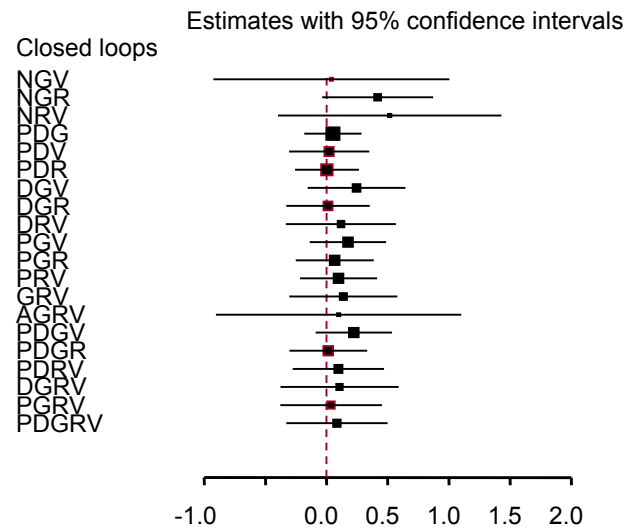
Inconsistency

Detecting

- Check the distribution of important characteristics per treatment comparison
 - Usually unobserved....
 - Time (of randomization, of recruitment) might be associated with changes to the background risk that may violate the assumptions of MTM
- Get a taste by looking for inconsistency in closed loops



Evaluation of concordance within closed loops



R routine in <http://www.dhe.med.uoi.gr/software.htm>

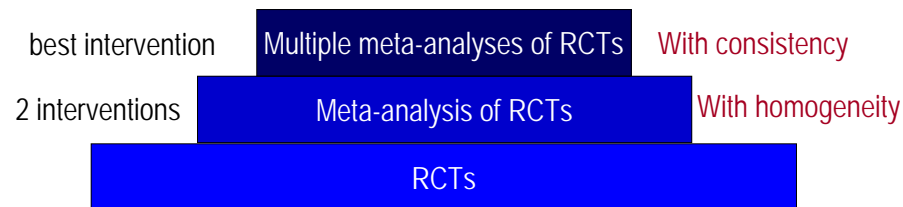
Salanti G, Marinho V, Higgins JP: A case study of multiple-treatments meta-analysis demonstrates that covariates should be considered. *J Clin Epidemiol* 2009, 62: 857-864.

Inconsistency

Detecting

- Check the distribution of important characteristics per treatment comparison
 - Usually unobserved....
 - Time (of randomization, of recruitment) might be associated with changes to the background risk that may violate the assumptions of MTM
- Get a taste by looking for inconsistency in closed loops
- Fit a model that relaxes consistency
 - Add an extra 'random effect' per loop (Lu & Ades JASA 2005)

Inconsistency - Heterogeneity



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